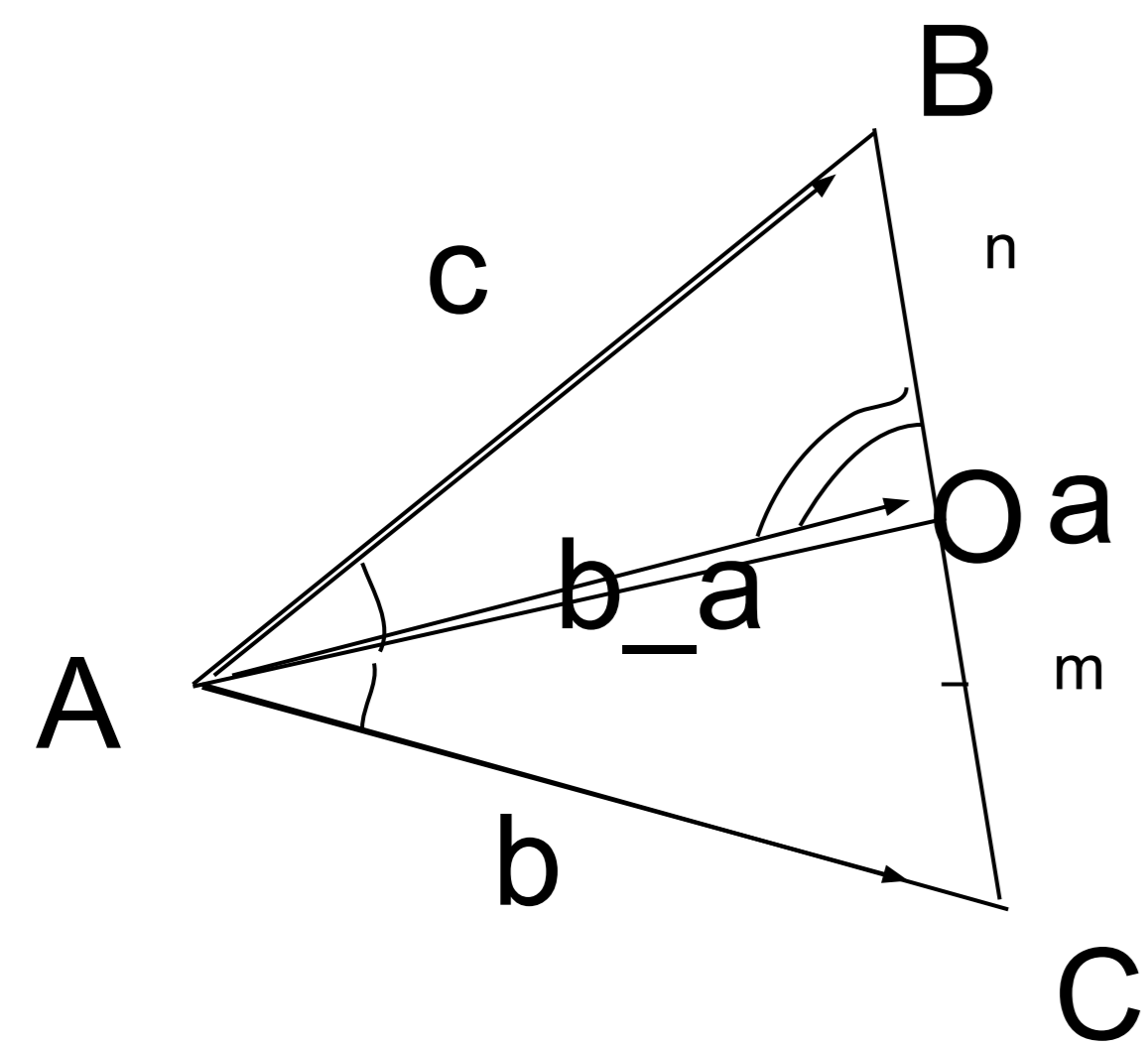
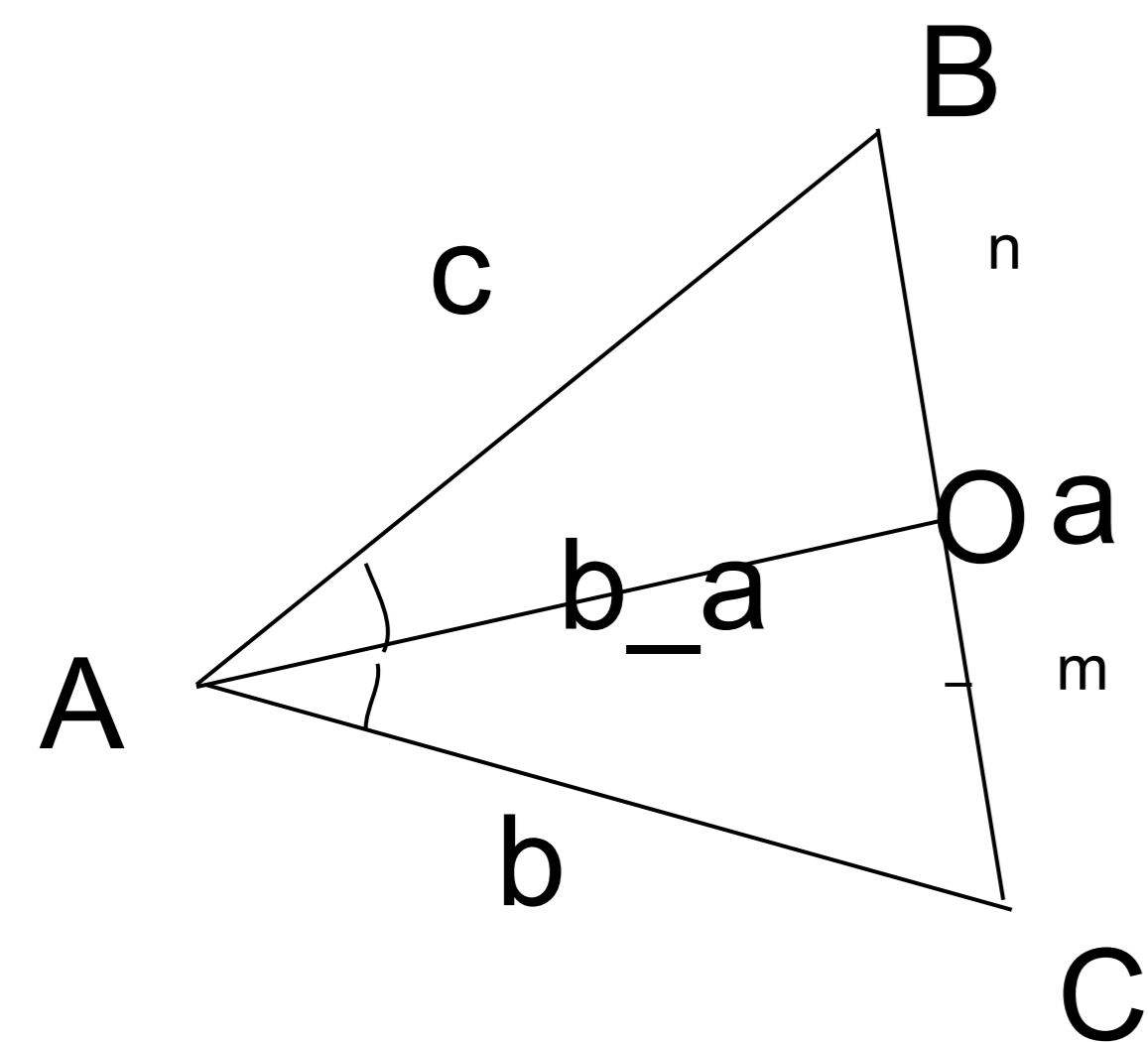
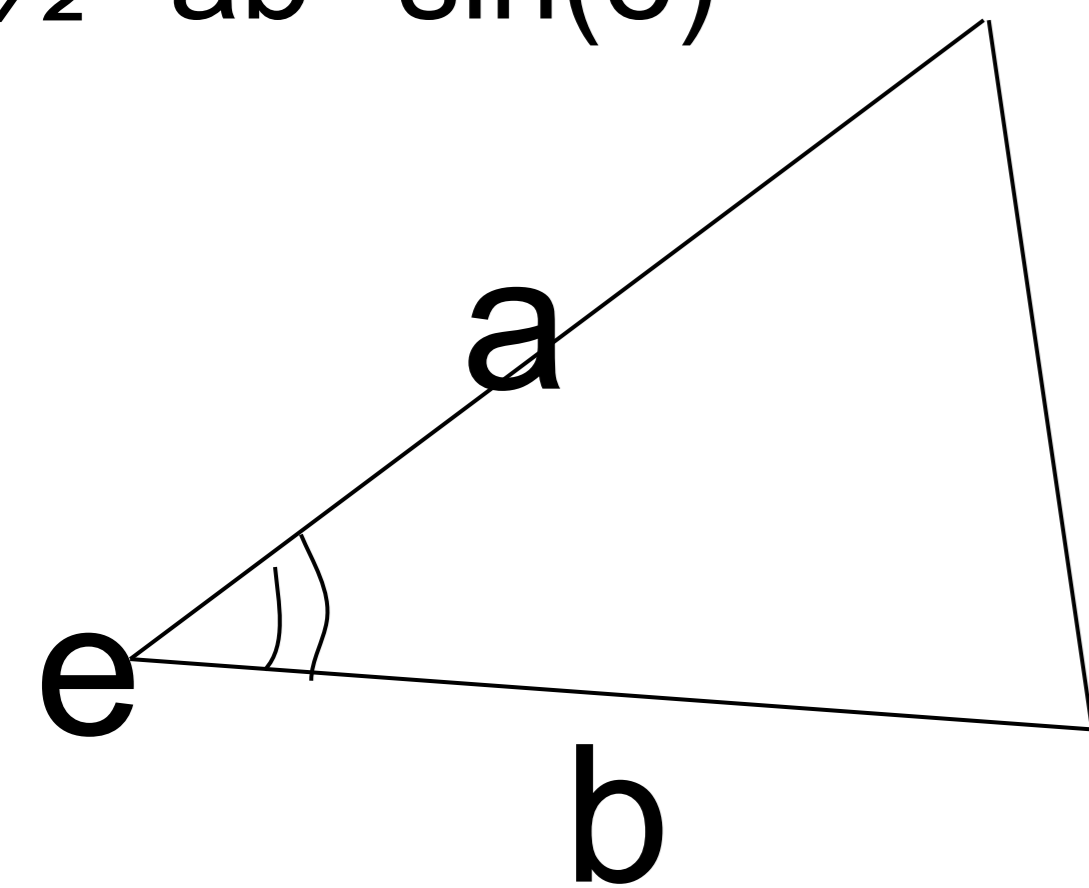


Дан треугольник ABC, и три его стороны a,b,c. найти b\_a



$$S = \frac{1}{2} * ab * \sin(e)$$



1 Метод:

$$\cos A = \frac{b^2 + c^2 - a^2}{2bc}$$

$$b_a / c = \cos\left(\frac{1}{2}(\arccos\left(\frac{b^2 + c^2 - a^2}{2bc}\right))\right)$$

$$b_a / \sin B = c / \sin(P - A/2 - B)$$

$$b_a = \sin B * c / \sin(P - A/2 - B)$$

2 Метод:

$$\sin(A/2)b_a * c + \sin(A/2)b_a * b = \sin A * c * d$$

$$\sin(A/2)b_a * (c + b) = \sin A * c * d$$

$$b_a = \sin A * c * d / (\sin(A/2) * (c + b))$$

$$b_a = 2 \cos(A/2) * c * d / (c + b)$$

$$\cos A = \frac{b^2 + c^2 - a^2}{2bc}$$

$$\cos A = 2 \cos^2(A/2) - 1$$

$$\cos(A/2) = \sqrt{\frac{\cos A + 1}{2}}$$

$$b_a = 2 \cos(A/2) * c * b / (c + b) = 2 \sqrt{\frac{\cos A + 1}{2}} * c * b / (c + b) = \frac{2cb}{c + b} * \sqrt{\frac{\cos A + 1}{2}} = \frac{2cb}{c + b} * \sqrt{\frac{\left(\frac{b^2 + c^2 - a^2}{2bc} + 1\right)}{2}}$$

$$= \frac{2cb}{c + b} * \sqrt{\frac{(b^2 + c^2 - a^2 + 2bc)/2bc}{2}} = \frac{2cb}{c + b} * \sqrt{\frac{(b + c)^2 - a^2}{4bc}}$$

$$= \frac{2cb}{c + b} * \sqrt{\frac{(b + c - a)(b + c + a)}{4bc}} = \frac{2cb}{c + b} * \sqrt{\frac{(p - a) * p}{bc}} = \frac{2 \sqrt{(p - a) * p * bc}}{c + b}$$